First Building Blocks For Implementations of Security Protocols Verified in Coq

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Motivation

- Long-term goal:
 - Verified implementation of a security protocol in Coq
- Results so far:
 - Important pieces of assembly and C code
 - Progress reports in other venues [SAC 2012, PLPV 2013]
 - Recently completed
- Why this presentation?
 - Much related work in verification of low-level code
 - Not that many examples of concrete pieces of code
 - Significant effort worth reusing

Concrete Verification Targets

- Pieces of code typical of security protocols
 - E.g., consider the SSL/TLS protocol:
 - <u>Core</u> = cryptographic schemes
 - Partly implemented in assembly
 - » Performance, security counter-measures
 - Mostly modular arithmetic:

Previous work

- » Modular exponentiation (e.g., all steps of ElGamal)
- » Pseudo-random number generation (key generation, probabilistic encryption)

This talk

- Extended GCD algorithm (e.g., inverse modulo for private keys of RSA)
- <u>Communication</u> = exchange of formatted binary packets
 - Parsing/pretty-printing
 - Usually implemented in C

Outline

- Formal verification of arithmetic functions
 - Case study: binary extended GCD
 - Formal verification of binary packet parsing
 - Case study: parsing of initialization packets for TLS
 - Related work and conclusion

Binary Extended GCD

Algorithm in Pseudo-code

- Extended? Given u and v, return $u * u_1 + v * u_2 = g * u_3 = GCD(u,v)$
- <u>Binary?</u> Multi-precision division → shifts
- Knuth's binary extended GCD ≈ 49 lines

```
WHILE x % 2 = 0 && y % 2 = 0 {
    x \leftarrow x / 2 ;
    y \leftarrow y / 2 ;
    g \leftarrow g \times 2 }.

Definition init
    u v u<sub>1</sub> u<sub>2</sub> u<sub>3</sub> v<sub>1</sub> v<sub>2</sub> v<sub>3</sub> t<sub>1</sub> t<sub>2</sub> t<sub>3</sub> :=
    u<sub>1</sub> \leftarrow 1 ;
    u<sub>2</sub> \leftarrow 0 ;
    u<sub>3</sub> \leftarrow u ;
    v<sub>1</sub> \leftarrow v ;
    v<sub>2</sub> \leftarrow 1 \rightarrow u ;
    v<sub>3</sub> \leftarrow v ;
    If u % 2 = 1 Then
```

 $t_1 \leftarrow 0$:

 $t_2 \leftarrow -1$;

 $t_3 \leftarrow - v$

 $t_1 \leftarrow 1$; $t_2 \leftarrow 0$; $t_3 \leftarrow u$.

Definition prelude x y g :=

```
THE CLASSIC WORK
NEWLY UPDATED AND REVISED

The Art of
Computer
Programming
VOLUME 2
Seminumerical Algorithms
Third Edition

DONALD E. KNUTH
```

```
 \begin{array}{l} \text{Definition begcd g u v } u_1 \, u_2 \, u_3 \, v_1 \, v_2 \, v_3 \, t_1 \, t_2 \, t_3 := \\ g \leftarrow 1 \; ; \\ \text{prelude u v g } ; \\ \text{init u v } u_1 \, u_2 \, u_3 \, v_1 \, v_2 \, v_3 \, t_1 \, t_2 \, t_3 \; ; \\ \text{WHILE } t_3 \neq 0 \; \{ \\ \text{WHILE } t_3 \% \; 2 = 0 \; \{ \; \text{halve u v } t_1 \, t_2 \, t_3 \; \} \; ; \\ \text{reset u v } u_1 \, u_2 \, u_3 \, v_1 \, v_2 \, v_3 \, t_1 \, t_2 \, t_3 \; ; \\ \text{subtract u v } u_1 \, u_2 \, u_3 \, v_1 \, v_2 \, v_3 \, t_1 \, t_2 \, t_3 \; \}. \\ \end{array}
```

```
\begin{array}{c} \text{Definition subtract} \\ \quad u \ v \ u_1 \ u_2 \ u_3 \ v_1 \ v_2 \ v_3 \ t_1 \ t_2 \ t_3 := \\ t_1 \leftarrow u_1 \ - \ v_1 \ ; \\ t_2 \leftarrow u_2 \ - \ v_2 \ ; \\ t_3 \leftarrow u_3 \ - \ v_3 \ ; \\ \text{If} \ 0 \ge t_1 \ \text{THEN} \\ \quad t_1 \leftarrow t_1 \ + \ v \ ; \\ \quad t_2 \leftarrow t_2 \ - \ u \\ \text{ELSE} \\ \quad \text{skip} \, . \end{array}
```

```
\begin{array}{c} \text{Definition reset} \\ \quad u \  \, v \  \, u_1 \  \, u_2 \  \, u_3 \  \, v_1 \  \, v_2 \  \, v_3 \  \, t_1 \  \, t_2 \  \, t_3 \ := \\ IF \  \, t_3 \geq 0 \  \, \text{THEN} \\ \quad u_1 \leftarrow t_1 \  \, ; \\ \quad u_2 \leftarrow t_2 \  \, ; \\ \quad u_3 \leftarrow t_3 \\ \\ ELSE \\ \quad v_1 \leftarrow v \  \, -t_1 \  \, ; \\ \quad v_2 \leftarrow - \  \, (u \  \, +t_2) \  \, ; \\ \quad v_3 \leftarrow -t_3. \end{array}
```

Binary Extended GCD From Pseudo-code to Assembly

```
 \begin{array}{l} \text{Definition begcd g u v } u_1 \, u_2 \, u_3 \, v_1 \, v_2 \, v_3 \, t_1 \, t_2 \, t_3 := \\ g \leftarrow 1 \; ; \\ \text{prelude u v g ;} \\ \text{init u v } u_1 \, u_2 \, u_3 \, v_1 \, v_2 \, v_3 \, t_1 \, t_2 \, t_3 \; ; \\ \text{While } t_3 \neq 0 \; \{ \\ \text{While } t_3 \% \; 2 = 0 \; \{ \; \text{halve u v } t_1 \, t_2 \, t_3 \; \} \; ; \\ \text{reset u v } u_1 \, u_2 \, u_3 \, v_1 \, v_2 \, v_3 \, t_1 \, t_2 \, t_3 \; \} \; ; \\ \text{subtract u v } u_1 \, u_2 \, u_3 \, v_1 \, v_2 \, v_3 \, t_1 \, t_2 \, t_3 \; \}. \\ \end{array}
```



```
Definition begcd_mips rk rg ru rv ru1 ru2 ru3
rv1 rv2 rv3 rt1 rt2 rt3 a0 a1 a2 a3 a4 a5 a6 a7 a8 a9 :=
 multi_one_u rk rg a<sub>0</sub> a<sub>1</sub> ;
 prelude_mips rk rg ru rv a<sub>0</sub> a<sub>1</sub> a<sub>2</sub> a<sub>3</sub>
 init_mips rk ru rv ru<sub>1</sub> ru<sub>2</sub> ru<sub>3</sub> rv<sub>1</sub> rv<sub>2</sub> rv<sub>3</sub>
                     rt<sub>1</sub> rt<sub>2</sub> rt<sub>3</sub> a<sub>0</sub> a<sub>1</sub> a<sub>2</sub> a<sub>3</sub> a<sub>4</sub> a<sub>5</sub> a<sub>6</sub>
 pick_sign rt3 a0 a1 ;
 WHILE (bne a<sub>1</sub> r0) {
   multi_is_even_s rt3 a0 a1 a2 ;
   WHILE (bne a_2 r0) {
     halve_mips rk ru rv rt1 rt2 rt3
                            a<sub>0</sub> a<sub>1</sub> a<sub>2</sub> a<sub>3</sub> a<sub>4</sub> a<sub>5</sub> a<sub>6</sub>;
     multi_is_even_s rt3 a0 a1 a2 }
   \texttt{reset\_mips} \ \texttt{rk} \ \texttt{ru} \ \texttt{rv} \ \texttt{ru}_1 \ \texttt{ru}_2 \ \texttt{ru}_3 \ \texttt{rv}_1 \ \texttt{rv}_2 \ \texttt{rv}_3
                         rt1 rt2 rt3 a0 a1 a2 a3 a4 a7 a8 a9
   subtract_mips rk ru rv ru1 ru2 ru3 rv1 rv2 rv3
                                rt1 rt2 rt3 a0 a1 a2 a3 a4 a5 a6 a7 a8
   pick_sign rt3 a0 a1 }.
```

(69 l.o.c of MIPS)

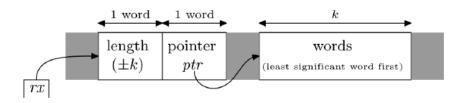
Main issue:

Arbitrary-size integers → Multi-precision integers (In other words, quid of overflows?)

"in many cases the intellectual heart of a program lies in the ingenious choice of data representation rather than in the abstract algorithm" (J.C. Reynolds, 1981)

Starting point:

Signed integers like in the celebrated GMP library



Library of verified arithmetic functions: Signed additions, subtraction, halving, doubling, etc. (25 functions, 313 l.o.c. of MIPS)

Pseudo-code \(\leftarrow\) Assembly

- \mathcal{R}_{\cdot} for arithmetic (e.g.): Forward simulation: rx ptr len registers Difficulties: overflows, special treatment of zeros memory pseudopseudocode assembly
- Compositional reasoning (e.g.):

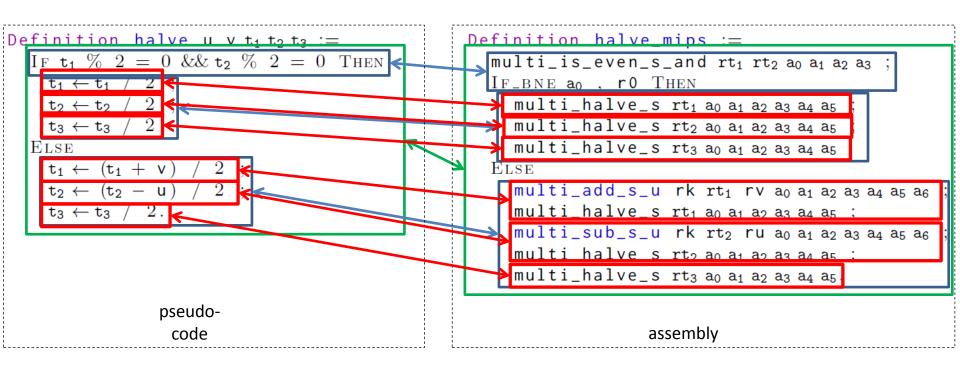
$$\frac{p \leq_{\mathcal{R}}^{\mathcal{P}} c \quad p' \leq_{\mathcal{R}}^{\mathcal{Q}} c'}{p;p' \leq_{\mathcal{R}}^{\mathcal{P}} c;c'} [\mathcal{P}]_{p} \downarrow_{c}[\mathcal{Q}]$$

code

assembly

Pseudo-code ←→ Assembly Simulation Proof

- 1. Decompose using compositional reasoning
- 2. Basic simulations proved using *support library*



Example: One of the five steps of the binary extended gcd

Binary Extended GCD in Assembly Technical Verification Overview

- Support library
 - Verification of basic functions for signed multi-precision arithmetic
 - Signed additions, substractions, halving, doubling, etc. (25 functions, 313 l.o.c. of MIPS)
 - Prove correctness (7,746 l.o.c. of Coq scripts)
 - Simulation statements (4,753 l.o.c. of Coq scripts)
- Application to Knuth's binary extended GCD
 - 1. Formal verification of the pseudo-code
 - Loop-invariants about functional correctness
 - 2. 1,466 l.o.c of *systematic* Coq scripts (for 69 l.o.c. of MIPS)
 - Invariants about implementation details only (overflows)
- Details:
 - [On Construction of A Library of Formally Verified Low-level Arithmetic Functions, ISSE 9(2): 59-77 (2013)]

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 - Case study: binary extended GCD
- Formal verification of binary packet parsing
 - Case study: parsing of initialization packets for TLS
 - Related work and conclusion

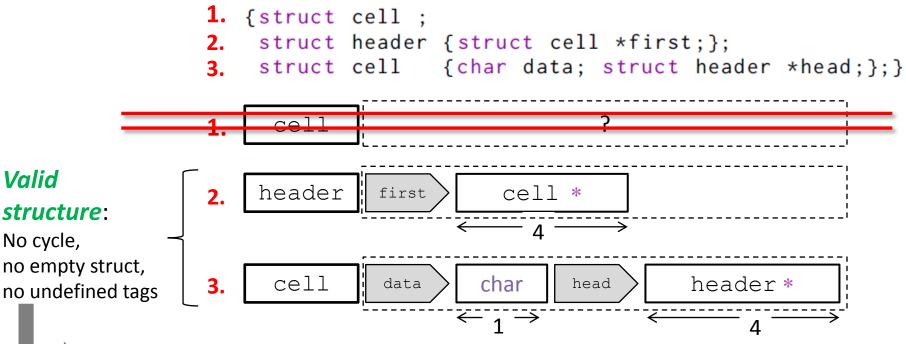
An Intrinsic Encoding of a subset of C

Expressions indexed with (type-checking rules for) C types:

```
Inductive exp \{g \ \sigma\}: g.-typ \rightarrow Type
               | var e : \forall str t, get str \sigma = \lfloor t \rfloor \rightarrow \exp t
  Variable
               | cst e : \forall t, t.-phy \rightarrow exp t
 Constant
                                                                                                     same
Arithmetic
               add_e : \forall t, exp (btyp: t) \rightarrow exp (btyp: t) \rightarrow exp (btyp: t)
  addition
                                                                                                     Notation "a Y+b" := ...
               add_p : \forall t, exp (:* t) \rightarrow exp (btyp: sint) \rightarrow exp (:* t)
                                                                                                     using
   Pointer
arithmetic
                                                                                                     Class/Instance
              Usefulness:
                                                                                %"buf" : exp (:* (btyp: uchar))
                            [ 1 ]<sub>sc</sub> : exp (btyp: sint)
                Arithmetic addition:
                                                        Pointer arithmetic:
                                                      %"buf" + [ 1 ]<sub>sc</sub>
                                                                                             %"buf" + %"buf"
                  [1]_{sc} + [1]_{sc}
```

Deep embedding of C Types

Example of a C structure:

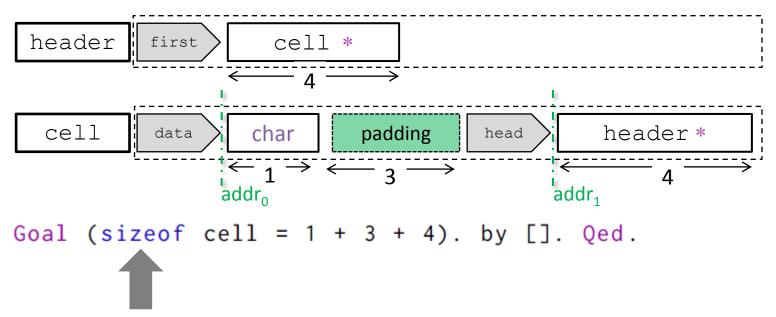


Generic terminating type traversal function:

```
Program Definition typ_traversal (ty : g.-typ) : Res :=
Record config {Res Accu : Type} := mkConfig {
  f_ityp : ityp -> Res ;
  f_ptyp : typ -> Res ;
  f_styp_iter : Accu -> string * g.-typ * Res -> Accu ;
  f_styp_fin : tag * g.-typ -> (Accu -> Accu) -> Res ;
  f_atyp : nat -> tag * g.-typ -> Res -> Res }.
```

Application to size of Computation

C structures are padded to conform to alignment:



Obtained by instantiating of the generic type traversal:

```
Definition sizeof_config g := mkConfig g
  sizeof_ityp
  (fun _ => sizeof_ptr)
  (fun a x => a + padd a (align x.1.2) + x.2)
  (fun ty a => a 0 + padd (a 0) (align ty.2))
  (fun s _ r => muln s r).
```

Application to Pretty-printing (new)

Pretty-printer = instantiation of the generic type traversal:

```
Definition pp_config {g} := (mkConfig g
  (fun t name tl => ityp_to_string t (" " ++ name ++ tl))
  (fun t name tl => typ_to_string t ("(*" ++ name ++ ")") tl)
  (fun accu p => accu ++ p.2 p.1.1 ("; "))
  (fun p f name tl => "struct " ++
    struct_tag_to_string p.1 (" { " ++ f "" ++ "} " ++ name ++ tl))
    (fun sz _ f name tl => f name ("[" ++ pp_nat sz ("]" ++ tl))))%string.
```

Example:

```
{struct cell ;
struct header {struct cell *first;};
struct cell {char data; struct header *head;};}

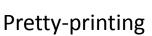
Goal PrintAxiom _ (typ_to_string_rec gcell "" "").
compute.

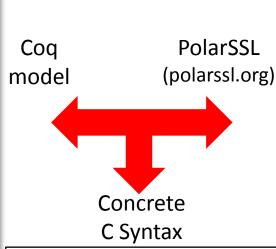
PrintAxiom string
"struct cell { unsigned char data; struct header (*head); } "
```

Case Study (1/2)

Parsing of Network Packets for SSL/TLS

```
efinition ssl parse client hello1 cont :=
 ret <-ssl fetch input( ssl, [ 5 ]sc);
If b[ ret \!= [ 0 ]sc ] Then
Else (
 _buf <-* __ssl .=> get_in_hdr ;
 _buf0 <-*__buf ;
If b[ ( buf0 \& [ 128 ]8uc) \!= [ 0 ]8uc ] Then
  ret <- [ POLARSSL ERR SSL BAD HS CLIENT HELLO ]c;
  ret
Else
      buf0 \!= [ SSL MSG HANDSHAKE ]c ] Then
   ret <- [ POLARSSL ERR SSL BAD HS CLIENT HELLO ]c ;
  ret
Else (
 buf1 <-* buf \+ [1]sc;
If b[ buf1 \!= [ SSL MAJOR VERSION 3 lc ] Then
   ret <- [ POLARSSL ERR SSL BAD HS CLIENT HELLO ]c ;
Else (
 buf3 <-* buf \+ [ 3 ]sc ;
 _buf4 <-* _buf \+ [ 4 ]sc ;
 If b[ _n \<e [ 45 ]sc ] Then
  ret <- [ POLARSSL ERR SSL BAD HS CLIENT HELLO ]c;
  ret
      n \>e [ 512 ]sc ] Then
  ret <- [ POLARSSL ERR SSL BAD HS CLIENT HELLO ]c ;
  ret
Else (
```



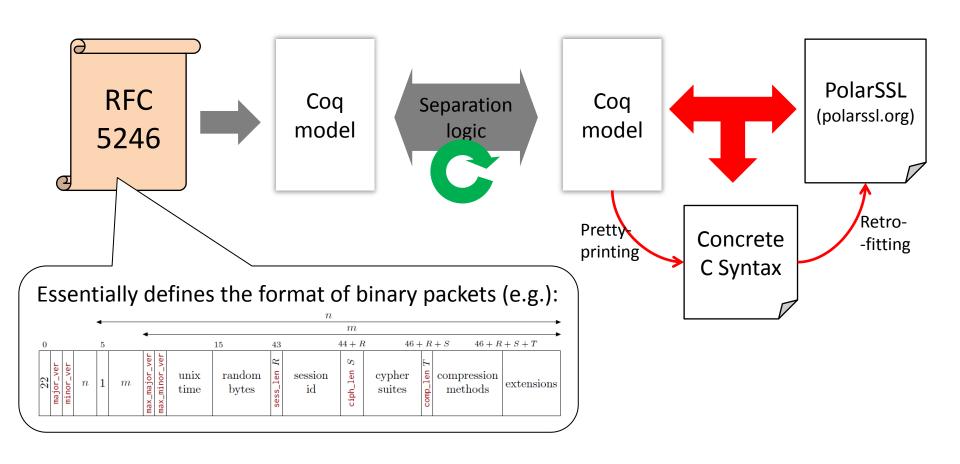


```
static int ssl parse client hello( ssl context *ssl )
    int ret, i, j, n;
   int ciph_len, sess_len;
int chal_len, comp_len;
    unsigned char *buf, *p;
    SSL DEBUG MSG( 2, ( "=> parse client hello" ) );
    if( ( ret = ssl_fetch_input( ssl, 5 ) ) != 0 )
        SSL DEBUG RET( 1, "ssl fetch input", ret );
        return( ret );
   buf = ssl->in hdr;
    if( ( buf[0] & 0x80 ) != 0 )
        SSL DEBUG BUF( 4, "record header", buf, 5 );
        SSL DEBUG MSG( 3, ( "client hello v2, message type: %d",
                        buf[2] ) );
        SSL_DEBUG_MSG( 3, ( "client hello v2, message len.: %d",
                        ( ( buf[0] & 0x7F ) << 8 ) | buf[1] ) );
        SSL DEBUG MSG( 3, ( "client hello v2, max. version: [%d:%d]",
                        buf[3], buf[4] ) );
         * SSLv2 Client Hello
```

```
"ret = ssl_fetch_input(ssl, 5);
if (((ret) != (0))) {
} else {
buf = *(ssl)->in hdr;
buf0_ = *buf;
if (((( buf0 ) & (128u)) != (0u))) {
ret = -38912;
if ((( buf0 ) != (22u))) {
ret = -38912;
} else {
 buf1 = *(buf) + (1);
if ((( buf1 ) != (3u))) {
ret = -38912;
} else {
buf3 = *(buf) + (3);
buf4 = *(buf) + (4);
\bar{n} = (((unsigned char)(\underline{buf3})) << (8)) | ((unsigned char)(\underline{buf4}));
if (((n) < (45))) {
ret = -38912;
} else {
if (((n) > (512))) {
ret = -38912;
} else {
```

Retrofitting

Case Study (2/2) Parsing of Network Packets for SSL/TLS



ClientHello Parsing (1/2) Technical Verification Overview

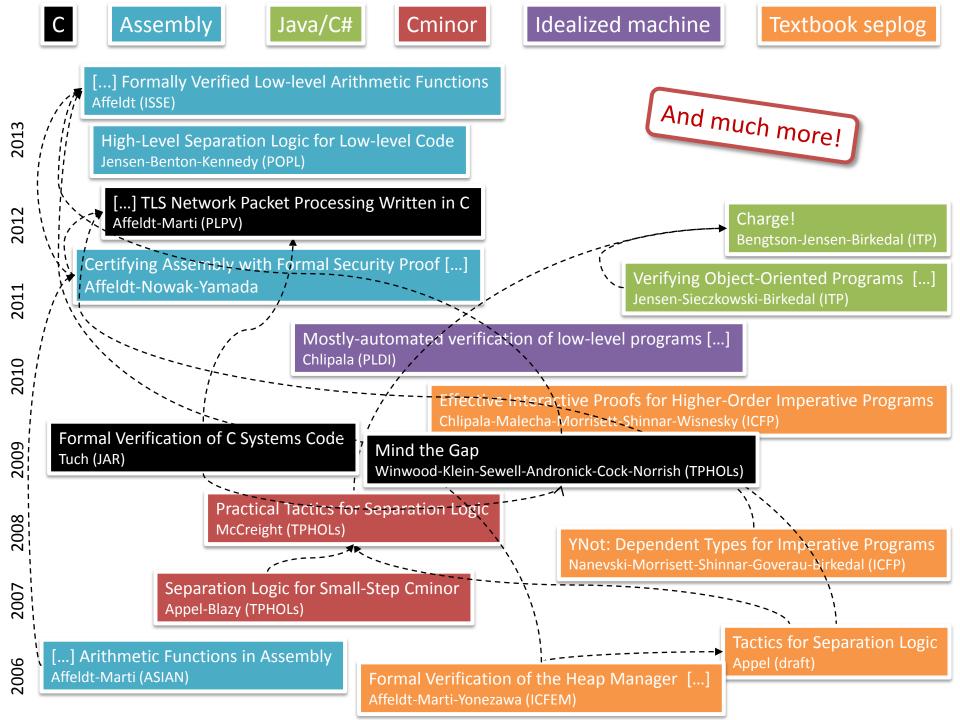
- Target function: ssl parse client hello
 - Original C code: 161 l.o.c. (85 w.o. comments and debug info)
 - Cog model: 132 l.o.c. (Patched version!)
 - goto → while
 - Expressions with side-effects → split into commands
- Formal proof:
 - 4087 l.o.c. (≈ 30 l.o.c. Coq scripts / l.o.c. of C)
 - Ltac tactics (a la Appel [2006])
 - Low-level manipulation of bit strings (shifts, concats, etc.) and overflow checking occupy much space
- Benefits of formal verification:
 - Debugging of the original C code:
 - To prevent accesses to allocated but not initialized memory
 - To guarantee conformance to RFC
 - Check for the absence of extensions
 - Restrictions w.r.t. RFC have been made explicit
 - Some features are not implemented (by design?), but which ones?

ClientHello Parsing (2/2) Technical Verification Overview

- Compilation of ssl parse client hello's proof:
 - $-\approx$ 220 min. (Unix time)
 - $-\approx 9$ GB of RAM
- Bottleneck:
 - Most time spent checking a nested loop (for cipher search)
 - Where Separation logic assertions are large because of invariants
- Counter-measures:
 - Hide string constants behind identifiers
 - Careful management of hypotheses
 - Rewrite Program functions by hand
 - lazy rather than compute
 - Ad-hoc lemmas rather than Ltac tactics
 - Trade-off short scripts ↔ compilation/maintenance time

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Conclusion

- Summary:
 - Formal verification of concrete pieces of low-level code
 - Arithmetic functions in assembly
 - Network packet processing in C
 - ⇒ Our work provides concrete clues about the verification of security protocols in Coq
- Development tarballs online:
 - http://staff.aist.go.jp/reynald.affeldt/coqdev
- Future work:
 - Enable verification of program mixing assembly and C